

A conditional extreme value model for severe storm environments

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Photo by Everett Nychka



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Severe Weather

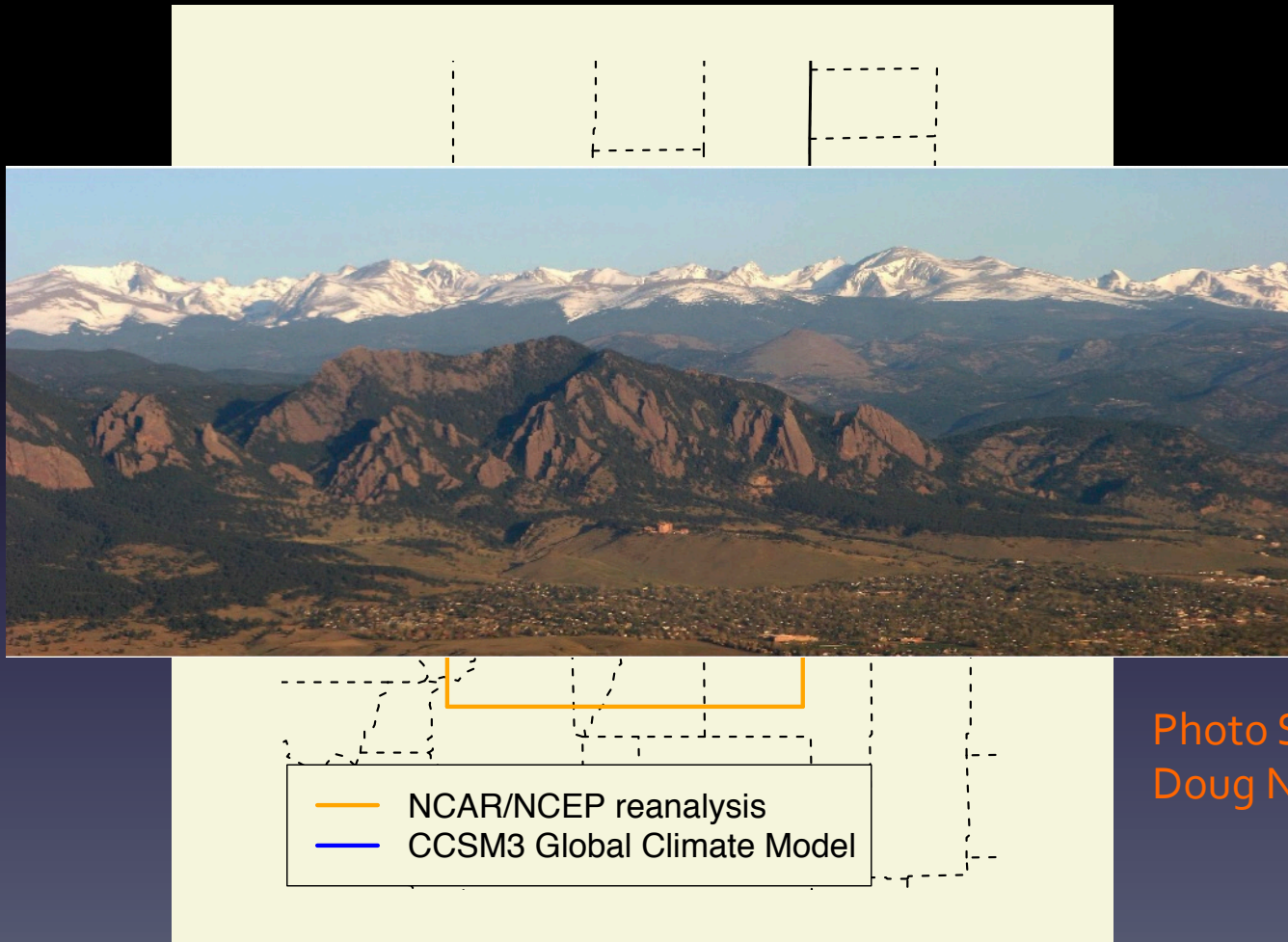


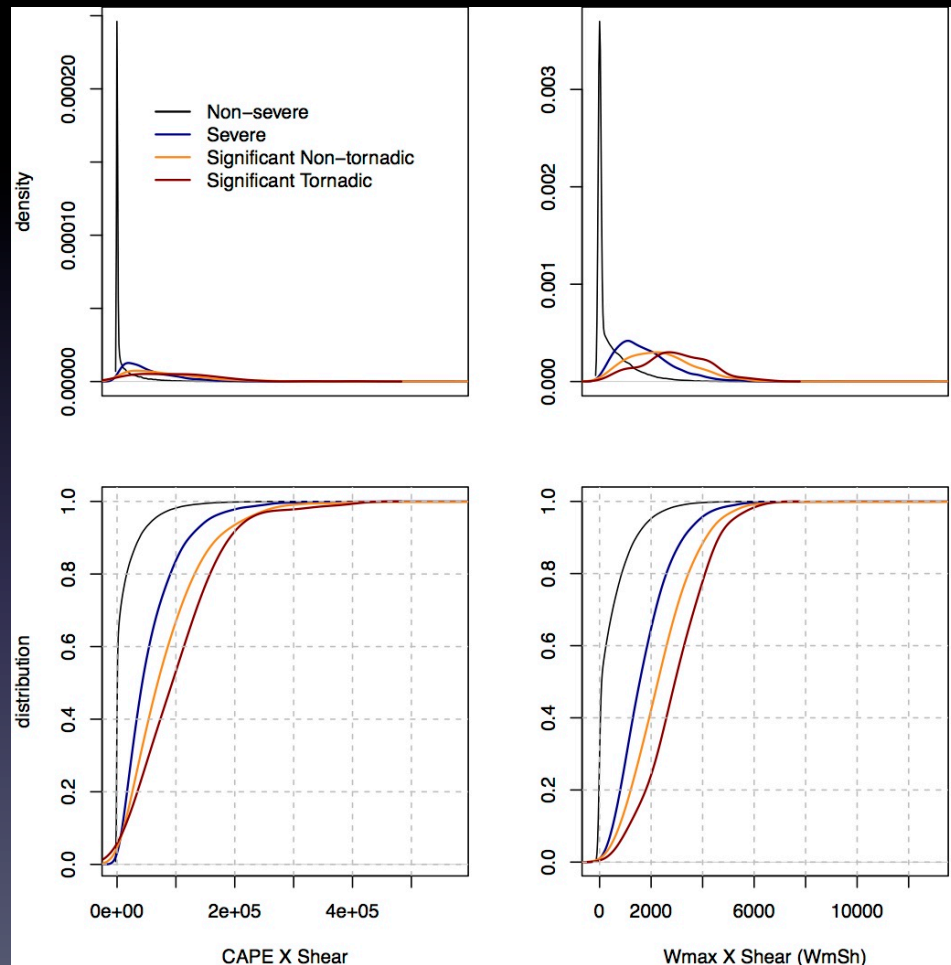
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Severe Storm Environments

CAPE (J/kg)



0 – 6 km Wind Shear (m/s)



Maximum updraft potential wind (Wmax, m/s)

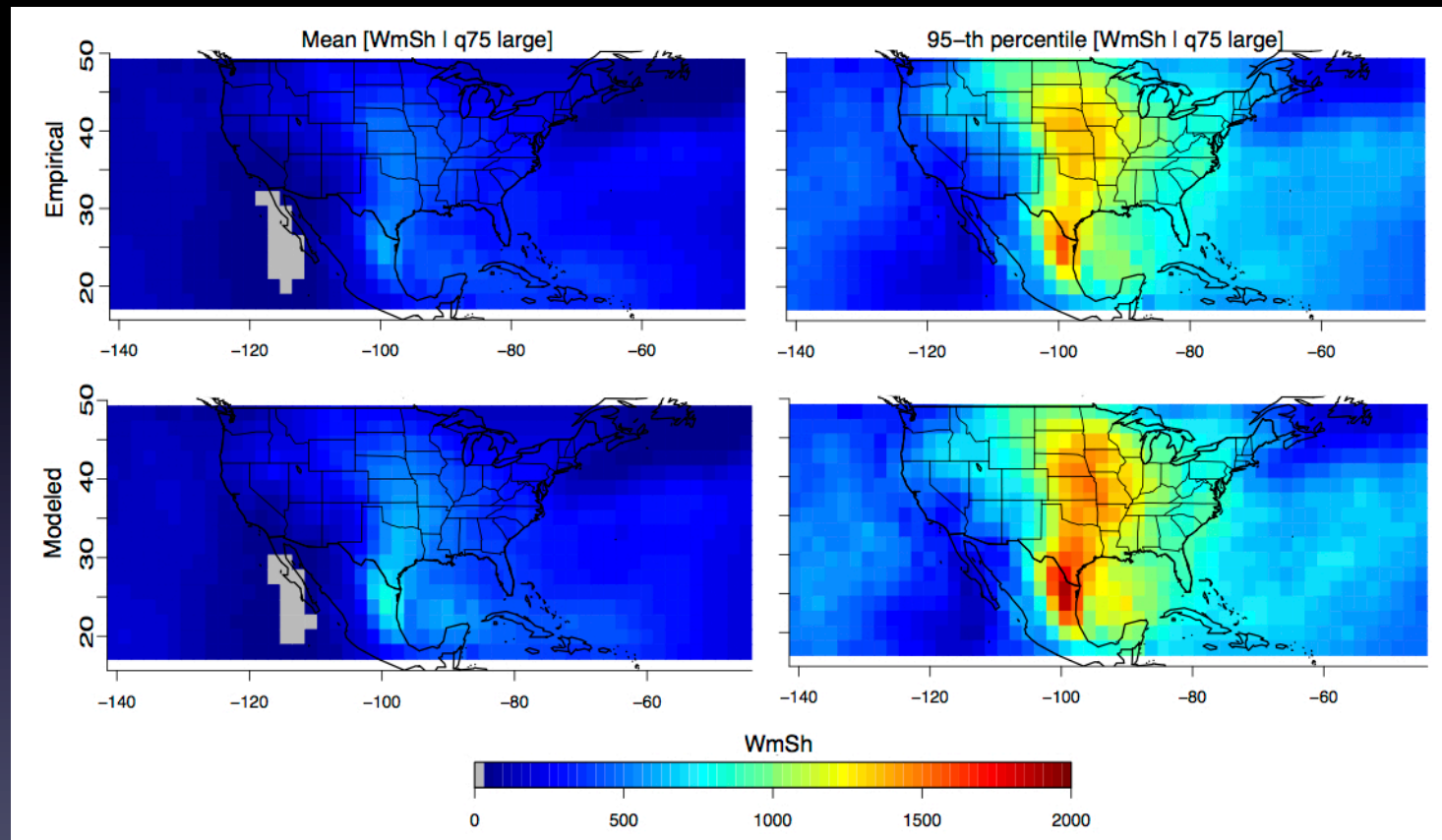


0 – 6 km Wind Shear (m/s)



WmSh (m²/s²)

Severe Storm Environments



WmSh (m²/s²) NCAR/NCEP Global Reanalysis (1958 – 1999)
884 station subset

Conditional Extreme Value Model

X, Y Laplace-transformed random variables, assume:

$$\Pr \left\{ Y > y, \frac{X - a(Y)}{b(Y)} \leq z \mid Y > u \right\} \xrightarrow{u \rightarrow \infty} \exp(-y) G(z)$$

$$a(Y) = \alpha Y$$

$$b(Y) = Y^\beta$$

$$(\alpha, \beta) \in [-1, 1] \times (-\infty, 1)$$

Heffernan and Tawn (2004, JRSS B, 66, 497 – 546)

Heffernan and Resnick (2007, Ann. Appl. Prob., 17, 537 – 571)

Keef et al. (2012, Environmetrics, doi: 10.1002/env.2190)

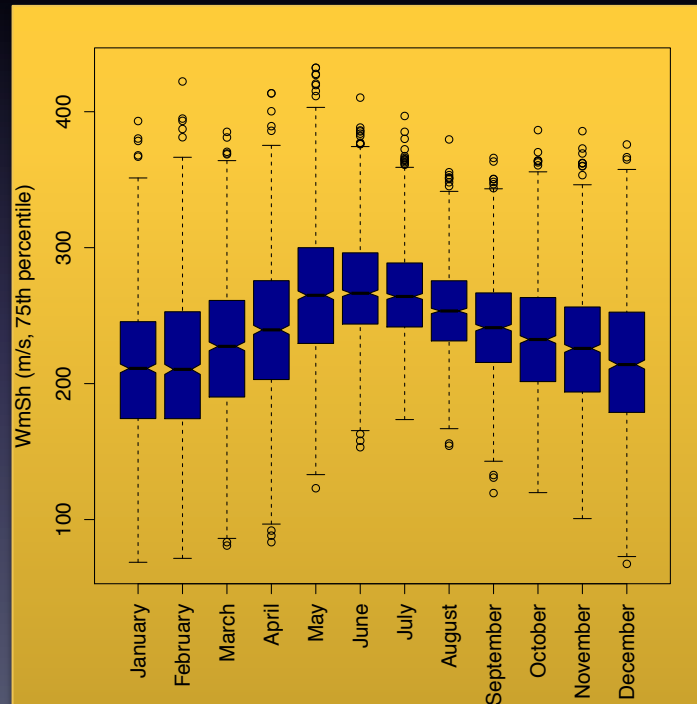
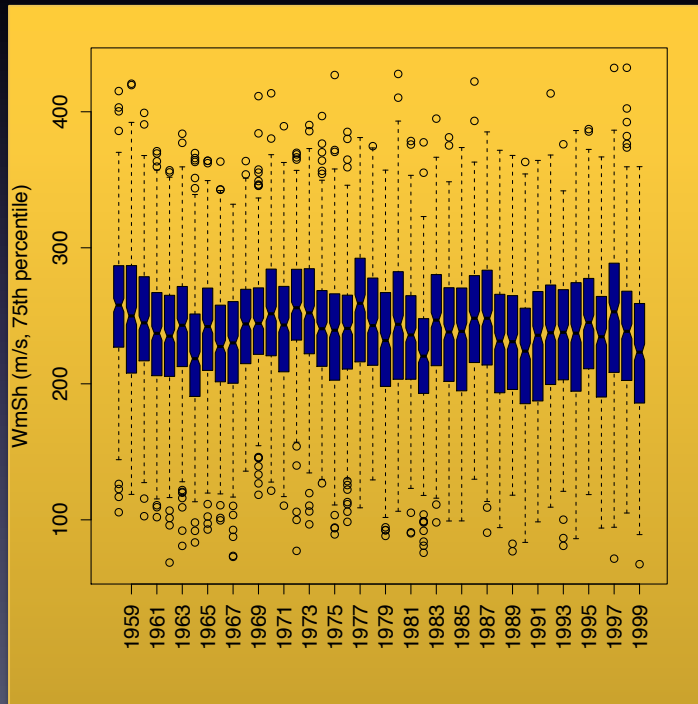
Conditional Extreme Value Model

$$\Pr \left\{ Y > y, \frac{X - a(Y)}{b(Y)} \leq z \mid Y > u \right\} \xrightarrow{u \rightarrow \infty} \exp(-y) G(z)$$

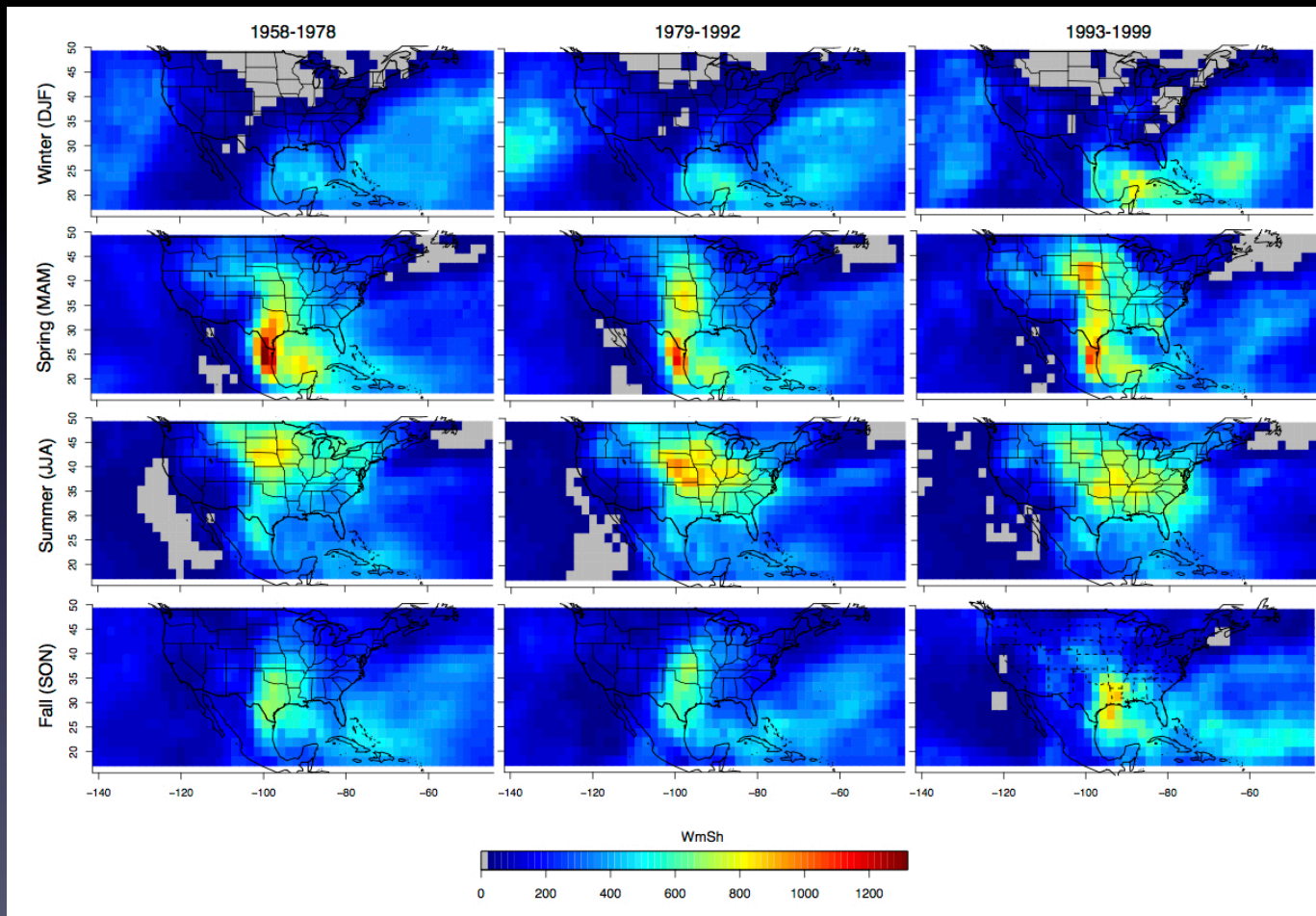

$$X_{|Y>u} = \alpha Y + Y^\beta Z_{|Y>u}$$

Conditional Extreme Value Model for Severe Storm Environments

Condition WmSh at each grid point on having "extreme energy" in the field

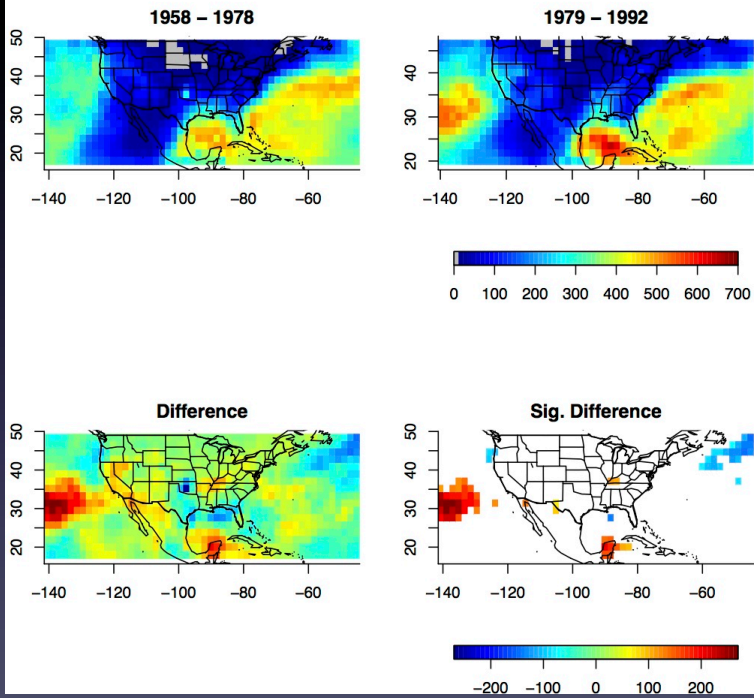


Conditional Extreme Value Model for Severe Storm Environments

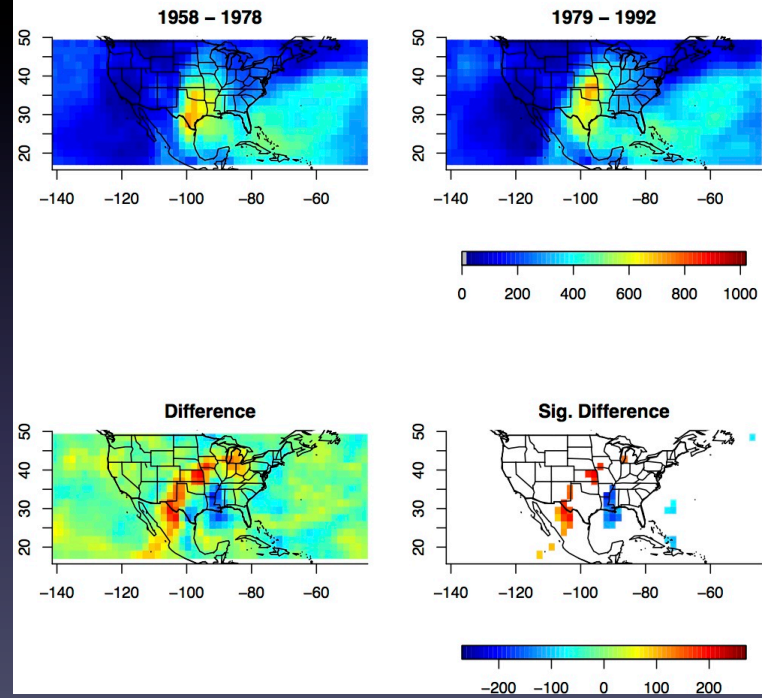


Conditional Extreme Value Model for Severe Storm Environments

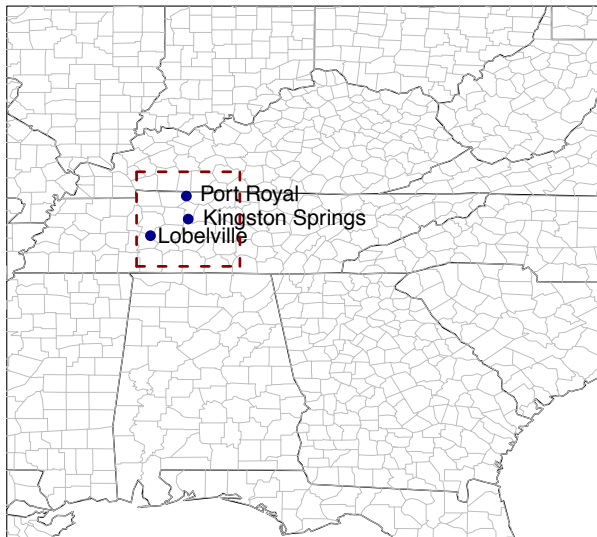
Winter



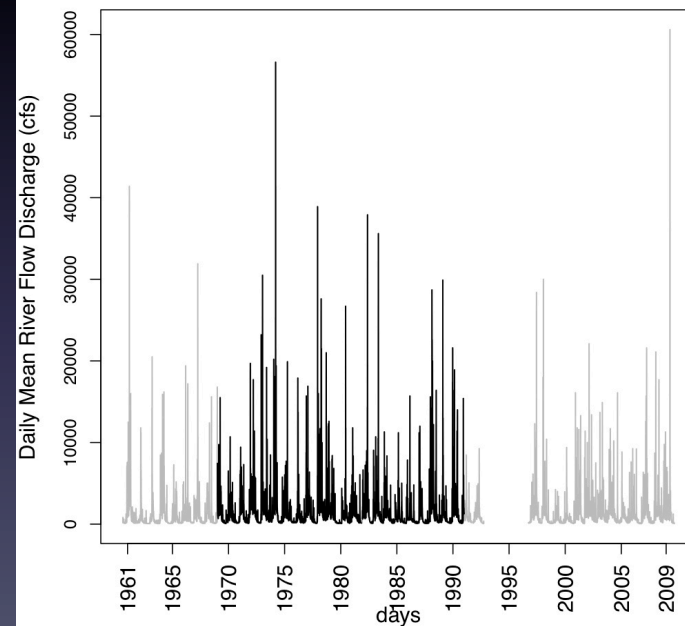
Fall



Conditional Extreme Value Model for Severe Storm Environments

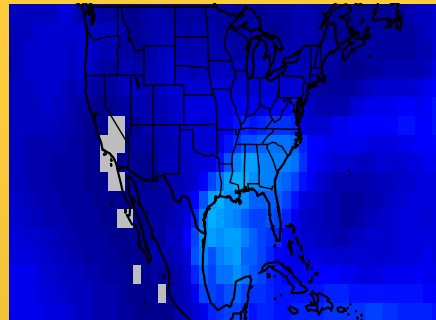


Red River at Port Royal, TN

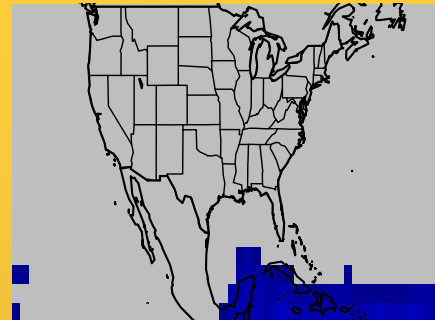


Conditional Extreme Value Model for Severe Storm Environments

WmSh (m^2/s^2)
conditioned on high
river flow (cfs)

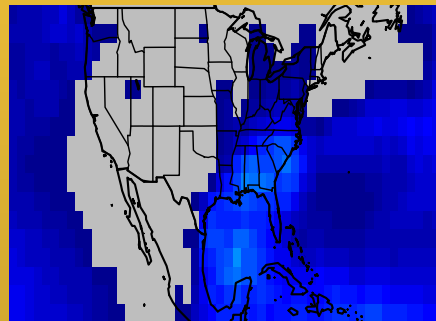


Mean

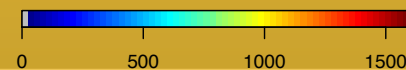
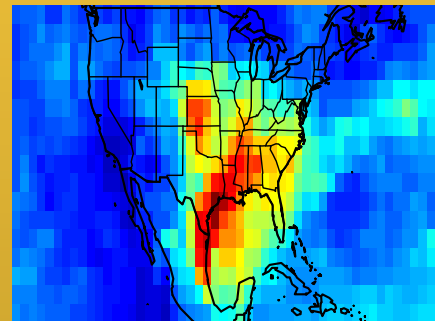


Lower 5-th percentile

Upper 95-th percentile

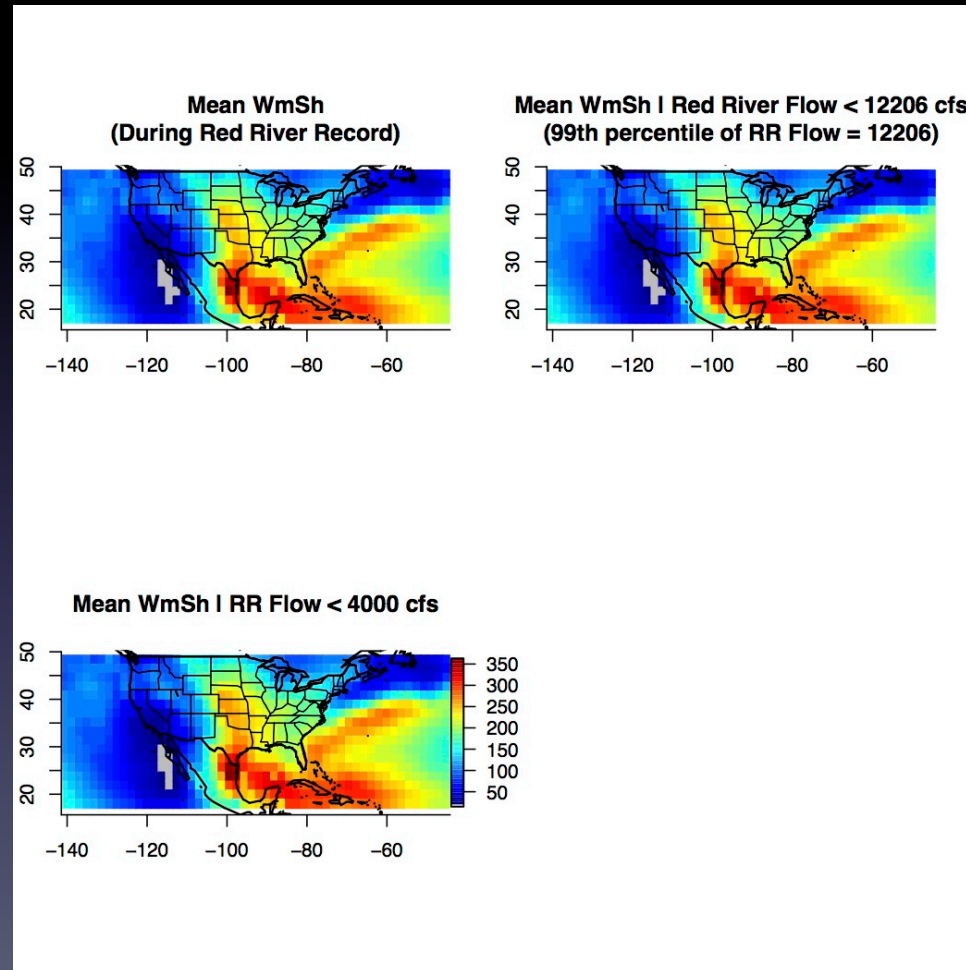


Median

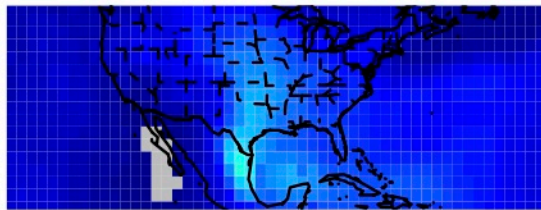


Conditional Extreme Value Model for Severe Storm Environments

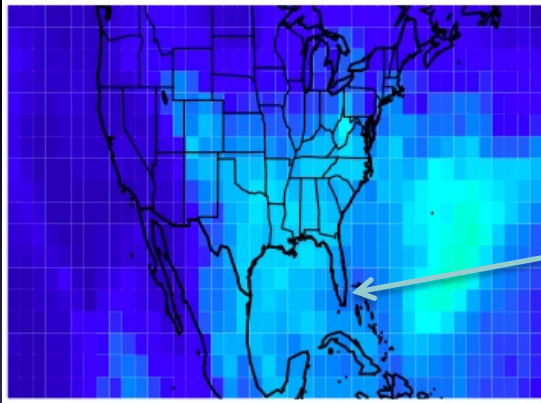
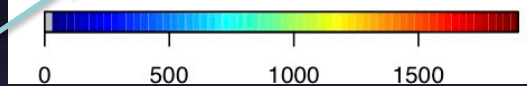
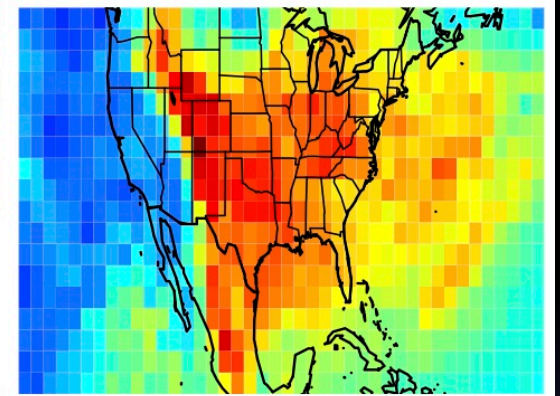
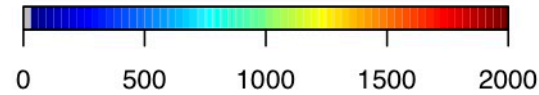
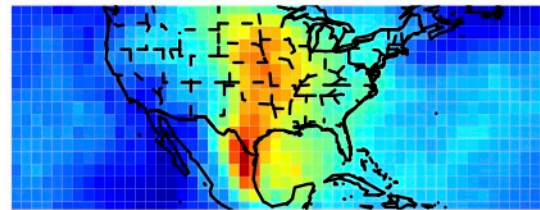
WmSh (m^2/s^2)
conditioned on lower
river flow (cfs)



Observed Reanalysis Mean
[WmSh | q75 > u]

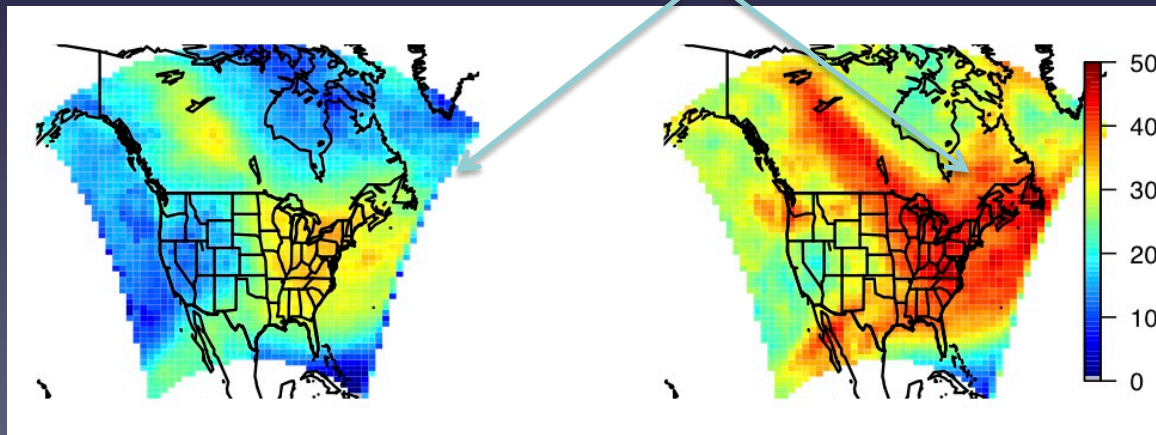


Observed Reanalysis 95-th
percentile [WmSh | q75 > u]



CCSM3 Global Climate Model

RCM3 Regional Climate Model



Summary and Future Work

- Use of large-scale indicators for severe storm environments is one way to project extremes in future climates without requiring high-resolution output
- Conditional EVA model introduced by Heffernan and Tawn provides a good way to model the extreme environments spatially (to examine the spatial structures that result)
- Could be useful for evaluating climate model output in terms of capturing extreme storm environments
- Can Estimation and Inference be improved?
 - empirical Bayes is showing promise here
- extRemes version 2.0 to be released soon.

Heffernan and Tawn conditional EVA model was fit using the R (<http://www.r-project.org>) package, texmex.

Image plots were made using the poly.image function from the R package, fields.